Sequences of evanescent solutions of semipositone problems in exterior domains

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We investigate the existence and multiplicity of positive stationary solutions for a certain class of convection-diffusion equations in exterior domains. This problem leads to the following elliptic equation $\Delta u(x) + f(x, u(x)) + g(x)x \cdot \nabla u(x) = 0$, for $x \in \Omega_R = \{x \in \mathbb{R}^n, ||x|| > R\}$, n > 2. Our goal is to show that the problem possesses nondecreasing sequences of solutions u satisfying the following condition: there exist 0 < A < B and L > 0 such that for all $x \in \mathbb{R}^n$, ||x|| > L, $A ||x||^{(2-n)} \le u(x) \le B ||x||^{(2-n)}$. The case when $f(x, \cdot)$ may be negative at the origin, so-called semipositone problem, is also considered. Our results are based on a certain iteration schema in which we apply the subsolution and supersolution method developed by Noussair and Swanson.

References

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1